# Phase Equilibrium Properties of the 1-Phenylethanol-Carbon Dioxide and 2-Octanol-Carbon Dioxide Binary Systems at 303.15 K, 313.15 K, and 323.15 K 

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#### Abstract

Phase equilibria data for the 1-phenylethanol $-\mathrm{CO}_{2}$ and 2-octanol $-\mathrm{CO}_{2}$ systems were measured at 303.15 $\mathrm{K}, 313.15 \mathrm{~K}$, and 323.15 K and at pressures up to 145 bar. An equilibrium cell with circulating gas phase was used for the measurements. Data were correlated with the Peng-Robinson equation of state. Different methods were tested for calculating the binary interaction parameters $\mathrm{k}_{\mathrm{ij}}$ and $\mathrm{I}_{\mathrm{ij}}$ of the quadratic mixing rules.


## Introduction

Vapor-liquid equilibrium (VLE) data for the 1-phenyle-thanol- $\mathrm{CO}_{2}$ and 2-octanol- $\mathrm{CO}_{2}$ systems are needed for enzymatic reactions using these substances as substrates. The substrates have to be dissolved in the $\mathrm{CO}_{2}$ stream which enters the reactor, where the enzyme is located and enzymatic reaction takes place. A knowledge of VLE data is important, because a good solubility of the substances in a wide range of pressure and temperature is desired so that the parameters for the reaction can be varied without encountering a limitation of substrate solubility.

The substances 1-phenyethanol and 2-octanol were measured, because few published data are available. Alwani and Schneider ${ }^{1}$ published $p(T)$ isopleths for the $\mathrm{CO}_{2}-$ 2-octanol system. For $\mathrm{CO}_{2}-1$-octanol, phase equilibria measurements were published by Weng and Lee ${ }^{2}$ in the temperature range from $40^{\circ} \mathrm{C}$ to $75^{\circ} \mathrm{C}$.

## Experimental Methods

Apparatus and Procedures. Phase equilibria experiments were performed in an equilibrium cell. The dynamic analytical method was used with circulation of the gas phase. The equilibrium cell (Figure 1) has a volume of 140 mL and is constructed for a maximum operating pressure of 400 bar at maximum temperature of $100^{\circ} \mathrm{C}$. Two sight glasses are installed in the front and back sides of the cell, which give a view into the cell over the whole height so that equilibrium phenomena can be observed. The $\mathrm{CO}_{2}{ }^{-}$ rich phase is withdrawn at the top of the cell, passes through a six-port HPLC valve with a sample loop of 200 $\mu \mathrm{L}$, and is recycled with a gear pump at the bottom of the cell. For better mixing and therefore faster equilibrium, the gas phase is circulated and a magnetic stirrer is placed in the center on the bottom of the cell. The whole system is placed in a thermostatted water bath and all pipes are thermostated to prevent separation of substances due to temperature gradients. Pressure and temperature in the cell are measured with accuracy of $\pm 0.1^{\circ} \mathrm{C}$ and $\pm 0.1$ bar.
$\mathrm{CO}_{2}$-Phase Sampling. During equilibrium time the $\mathrm{CO}_{2}$-phase passes through the sample loop. Thirty minutes before sampling, the stirrer and circulation of the gas phase

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Figure 1. High-pressure equilibrium cell for determining phase behavior: 1, calibrated glass cylinder; 2, liquid-phase sampling; 3, equilibrium cell; 4, six-port HPLC valve with $200 \mu \mathrm{~L}$ sample loop; 5, gear pump.
are switched off to prevent withdrawing of fine liquid droplets into the sample loop. A sample of the $\mathrm{CO}_{2}$ phase is taken by switching the six-port HPLC valve and expanding the volume of the sample loop into about $2-3 \mathrm{~mL}$ of ethanol situated in a calibrated $5-\mathrm{mL}$ flask, which is placed in ice water in order to collect all of the sample. After expansion, the sample loop is washed with ethanol and cleaned with compressed air to collect the whole sample which separates in the sample loop. The ethanol-sample mixture is filled with ethanol to exactly 5 mL , and this mixture is analyzed by a gas chromatographic method.

Liquid-Phase Sampling. For determining the dilute $\mathrm{CO}_{2}$ in the liquid phase, a sample is withdrawn from the bottom of the equilibrium cell and expanded into a glass vial which is weighed before and after sampling. The volume of the expanded liquid sample is about $1-2 \mathrm{~mL}$ so that the amount of dissolved $\mathrm{CO}_{2}$ in the liquid sample under atmospheric conditions can be neglected. The expanded $\mathrm{CO}_{2}$ leaves the glass vial at the top and enters a calibrated glass cylinder filled with water of a pH value of about 0.5 to limit solubility of $\mathrm{CO}_{2}$ in the water. From the measured water volume, the temperature and the pressure of the water bath, and the weight of sample in the glass vial, the amount of solved $\mathrm{CO}_{2}$ in liquid phase is calculated.
$\mathrm{CO}_{2}$-Density Calculation. The density of pure $\mathrm{CO}_{2}$ as a function of pressure and temperature was calculated with

Table 1. Isothermal Vapor-Liquid Equilibrium Data for the Carbon Dioxide (1)-1-Phenylethanol (2) System

| Pexp/bar | $\mathrm{X}_{1}$ | $\mathrm{Y}_{1}$ | Pexp/bar | $\mathrm{X}_{1}$ | $\mathrm{Y}_{1}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{~T}=303.15 \mathrm{~K}$ |  |  |  |  |  |  |
| 48 | 0.6240 | 0.9843 | 80 | 0.8650 | 0.9754 |  |
| 56 | 0.7050 | 0.9827 | 85 | 0.8795 | 0.9727 |  |
| 59 | 0.7400 | 0.9816 | 89 | 0.8900 | 0.9708 |  |
|  | $\mathrm{~T}=313.15 \mathrm{~K}$ |  |  |  |  |  |
| 35 | 0.3890 | 0.9937 | 117 | 0.8920 | 0.9766 |  |
| 67 | 0.6800 | 0.9871 | 119 | 0.8960 | 0.9762 |  |
| 83 | 0.7890 | 0.9840 | 122 | 0.8990 | 0.9756 |  |
| 90 | 0.8000 | 0.9830 | 125 | 0.9110 | 0.9748 |  |
|  |  | $\mathrm{~T}=323.15 \mathrm{~K}$ |  |  |  |  |
| 40 | 0.3600 | 0.9970 | 79 | 0.6631 | 0.9926 |  |
| 46 | 0.4290 | 0.9971 | 120 | 0.8030 | 0.9858 |  |
| 48 | 0.4490 | 0.9965 | 132 | 0.8431 | 0.9830 |  |
| 50 | 0.4870 | 0.9962 | 137 | 0.8546 | 0.9806 |  |
| 74 | 0.6290 | 0.9932 | 145 | 0.8952 | 0.9773 |  |
| 75 | 0.6302 | 0.9936 |  |  |  |  |

Table 2. Isothermal Vapor-Liquid Equilibrium Data for the Carbon Dioxide (1)-2-Octanol (2)-System

| Pexp/bar | $\mathrm{X}_{1}$ | $\mathrm{Y}_{1}$ | Pexp/bar | $\mathrm{X}_{1}$ | $\mathrm{Y}_{1}$ |  |
| :---: | :--- | :--- | :--- | :--- | :--- | :---: |
| $\mathrm{~T}=303.15 \mathrm{~K}$ |  |  |  |  |  |  |
| 30 | 0.4172 | 0.9984 | 55 | 0.723 | 0.9975 |  |
| 44 | 0.6047 | 0.9985 | 62 | 0.8246 | 0.9961 |  |
| 48 | 0.6411 | 0.9984 | 63 | 0.8425 | 0.9965 |  |
| 51 | 0.654 | 0.9981 | 65 | 0.901 | 0.9962 |  |
|  | $\mathrm{~T}=313.15 \mathrm{~K}$ |  |  |  |  |  |
| 44 | 0.517 | 0.9964 | 66 | 0.7305 | 0.9943 |  |
| 52 | 0.578 | 0.9954 | 71 | 0.774 | 0.9941 |  |
| 53 | 0.588 | 0.9944 | 76 | 0.837 | 0.9938 |  |
| 56 | 0.6553 | 0.9944 | 78 | 0.815 | 0.9928 |  |
| 64 | 0.6629 | 0.9938 | 80 | 0.9035 | 0.9936 |  |
| 65 | 0.6661 | 0.9948 | 81 | 0.9099 | 0.9936 |  |
|  |  | $=323.15 \mathrm{~K}$ |  |  |  |  |
| 22 | 0.255 | 0.9957 | 81 | 0.76 | 0.9892 |  |
| 46 | 0.4929 | 0.994 | 88 | 0.7876 | 0.9879 |  |
| 62 | 0.6156 | 0.9921 | 89 | 0.8226 | 0.9867 |  |
| 71 | 0.671 | 0.991 | 91 | 0.825 | 0.9866 |  |
| 72 | 0.645 | 0.9905 |  |  |  |  |

the Bender ${ }^{3,4}$ equation. The amount of $\mathrm{CO}_{2}$ in the sample loop for vapor-phase sampling and in the calibrated glass cylinder for liquid-phase sampling could be cal culated with a knowledge of density calculated with this equation.

Gas Chromatographic Method. The ethanol mixture from the $\mathrm{CO}_{2}$-phase sampling process is analyzed in a gas chromatograph (HP 5890 series II) with a flame ionization detector (GC-FID) using a capillary column (type DB-5, 25 $\mathrm{m} \times 0.32 \mathrm{~mm} \times 0.58 \mu \mathrm{~m})$. The injector temperature is held constant at $250^{\circ} \mathrm{C}$, and detector temperature is at $350^{\circ} \mathrm{C}$. The oven temperature is kept constant for 1 min at 100 ${ }^{\circ} \mathrm{C}$, increased by $25^{\circ} \mathrm{C} \cdot \mathrm{min}^{-1}$ up to $150^{\circ} \mathrm{C}$, and then is held constant for another 2 min . A calibration with different amounts of 1-phenylethanol and 2-octanol in ethanol was done to determine the calibration line and retention times of the substances.

Materials. 1-Phenylethanol (purity >98\%), 2-octanol (purity $>97 \%$ ), and ethanol (purity $>99.8 \%$ ) were supplied by Merck. The carbon dioxide with a purity $>99.94 \%$ and a dew point lower than $-60^{\circ} \mathrm{C}$ was purchased from Linde (Graz) and stored in a tank with a capacity of 3200 L.

## Results

In Table 1 we have given our original, unsmoothed data for the $\mathrm{CO}_{2}-1$-phenylethanol system and in Table 2 for the $\mathrm{CO}_{2}$-2-octanol system at $303.15 \mathrm{~K}, 313.15 \mathrm{~K}$, and 323.15 K . These data have been correlated by using the Peng-

Table 3. Critical Parameters $\mathrm{T}_{\mathrm{c}}$ and $\mathrm{P}_{\mathrm{c}}$ and Acentric Factor $\omega$ of the Pure Substances

|  | $\mathrm{MW} / \mathrm{g} \mathrm{mol}^{-1}$ | $\mathrm{~T}_{\mathrm{C}} / \mathrm{K}$ | $\mathrm{P}_{\mathrm{C}} /$ bar | $\omega$ |
| :--- | :---: | :---: | :--- | :---: |
| $\mathrm{CO}_{2}$ | 44.01 | 304.21 | 73.795 | 0.2250 |
| 1-phenylethanol | 122.17 | 686.03 | 40.93 | 0.7806 |
| 2-octanol | 130.23 | 613.66 | 27.53 | 0.7506 |

Table 4. Optimized $\mathrm{k}_{\mathrm{ij}}$ and $\mathrm{I}_{\mathrm{ij}}$ Values of the Carbon Dioxide (1)-1-Phenylethanol (2) and Carbon Dioxide (1)-2-Octanol (3) Systems

| method | $\mathrm{k}_{12}$ | $\mathrm{I}_{12}$ | $\mathrm{k}_{13}$ | $\mathrm{I}_{13}$ |
| :---: | :---: | :---: | :---: | :---: |
| 1 | -0.0169 |  | 0.0398 |  |
| 2 | -0.0172 | 0.0038 | 0.0430 | 0.0070 |

Table 5. $\Delta P / \%$ Values in the Predicted Bubble Point Pressure and Mean Deviation $\Delta Y$ between Experimental and Calculated Vapor Composition for the Carbon Dioxide (1)-1-Phenyethanol (2) System

|  | method1 |  |  | method 2 |  |
| :--- | :---: | :---: | :--- | :---: | :---: |
| temp/K | $\Delta \mathrm{P} / \%$ | $\Delta \mathrm{Y}$ |  | $\Delta \mathrm{P} / \%$ | $\Delta \mathrm{Y}$ |
| 303.15 | 5.91 | 0.0166 |  | 5.00 | 0.0164 |
| 313.15 | 1.75 | 0.0077 |  | 2.39 | 0.0078 |
| 323.15 | 3.69 | 0.0054 |  | 3.47 | 0.0055 |
| av | 3.60 | 0.0088 |  | 3.49 | 0.0088 |

Robinson equation of state ${ }^{5}$

$$
\begin{equation*}
P=\frac{R T}{V-b}-\frac{a(T)}{V(V+b)+b(V-b)} \tag{1}
\end{equation*}
$$

where $P$ is the pressure, $R$ is the gas constant, $T$ is the temperature, and V is the molecular volume. Different methods for calculating the parameter $b$ and the temper-ature-dependent function a were used to correlate the data with the van der Waals one-fluid mixing rules.

Method 1. For parameter a a quadratic mixing rate was used, and for b a linear mixing rule was used.

$$
\begin{gather*}
a=\sum_{i} \sum_{j} x_{i} x_{j} a_{i j}  \tag{2}\\
b=\sum_{i} x_{i} b_{i}  \tag{3}\\
a_{i j}=\left(a_{i j} a_{j j}\right)^{0,5}\left(1-k_{i j}\right) \tag{4}
\end{gather*}
$$

Method 2. Parameter a was calculated with eqs 2 and 4, but parameter b was calculated with a quadratic mixing rule

$$
\begin{equation*}
\mathrm{b}=\sum_{\mathrm{i}} \sum_{\mathrm{j}} \mathrm{x}_{\mathrm{i}} \mathrm{x}_{\mathrm{j}} \mathrm{~b}_{\mathrm{ij}} \tag{5}
\end{equation*}
$$

where

$$
\begin{equation*}
\mathrm{b}_{\mathrm{ij}}=\left(\frac{\mathrm{b}_{\mathrm{ij}}+\mathrm{b}_{\mathrm{jj}}}{2}\right)\left(1-\mathrm{l}_{\mathrm{ij}}\right) \tag{6}
\end{equation*}
$$

Table 3 gives the critical data $T_{C}$ and $P_{C}$ and the acentric factor $\omega$ of the pure components used with the PengRobinson equation of state. The values of the interaction parameters $\mathrm{k}_{\mathrm{ij}}$ and $\mathrm{I}_{\mathrm{ij}}$ were optimized by minimizing the $\Delta \mathrm{P} / \%$ values in the predicted bubble point pressure by using the experimental temperature, pressures, and liquidphase compositions.

$$
\begin{equation*}
\Delta \mathrm{P} / \%=\frac{100}{\mathrm{n}} \sum_{i=1}^{n} \frac{\left|\mathrm{P}_{\mathrm{i}}^{\exp }-\mathrm{P}_{\mathrm{i}}^{\mathrm{calc}}\right|}{\mathrm{P}_{\mathrm{i}}{ }^{\exp }} \tag{7}
\end{equation*}
$$

Table 6. $\Delta P / \%$ Values in the Predicted Bubble Point Pressure and Mean Deviation $\Delta \mathbf{Y}$ between Experimental and Calculated Vapor Composition for the Carbon Dioxide (1)-2-Octanol (2) System

|  | method 1 |  |  | method 2 |  |
| :--- | :---: | :---: | :--- | :---: | :---: |
| temp/K | $\Delta \mathrm{P} / \%$ | $\Delta \mathrm{Y}$ |  | $\Delta \mathrm{P} / \%$ | $\Delta \mathrm{Y}$ |
| 303.15 | 1.64 | 0.0024 |  | 1.62 | 0.0024 |
| 313.15 | 2.85 | 0.0051 |  | 2.99 | 0.0051 |
| 323.15 | 3.46 | 0.0084 |  | 3.22 | 0.0084 |
| av | 2.71 | 0.0054 |  | 2.68 | 0.0054 |



Figure 2. Pressure-composition diagram including experimental data and calculated with method 2 for the $\mathrm{CO}_{2}(1)-1$-phenylethanol (2) system at $303.15 \mathrm{~K}, 313.15 \mathrm{~K}$, and 323.15 K .


Figure 3. Pressure-composition diagram including experimental data and calculated with method 2 for the $\mathrm{CO}_{2}$ (1)-2-octanol (2) system at $303.15 \mathrm{~K}, 313.15 \mathrm{~K}$, and 323.15 K .

All calculations were done with the program OHGFOR developed by Professor Evelyne Neau of the Laboratoire de Chimie Physique, Marseille, France.
Optimized values of the interaction parameters $\mathrm{k}_{12}$ and $I_{12}$ for the different methods are given in Table 4. The $\Delta P / \%$ values and the mean deviation between experimental and calculated vapor composition $\Delta y$ for the different calculation methods as well for each temperature and also for the average of the three calculated temperatures are given in Tables 5 and 6 . From the $\Delta \mathrm{P} / \%$ values, it is obvious that
both methods result in the same accuracy and thus the quadratic mixing rule for parameter b brings no benefit.

The Peng-Robinson equation of state provided a fairly good representation of the VLE data for these systems as shown in the pressure composition diagrams, Figures 2 and 3, which depict both the experimental data and the calculated results of method 2.

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## Glossary

a,b parameters in Peng-Robinson equation of state
$\mathrm{k}_{\mathrm{ij}}, \mathrm{l}_{\mathrm{ij}} \quad$ binary interaction parameters
P pressure
T temperature
$x \quad$ mole fraction $\mathrm{CO}_{2}$ in the liquid phase
$y \quad$ mole fraction $\mathrm{CO}_{2}$ in the vapor phase
Greek Letters
$\Delta$
difference between experimental and calculated value
$\omega$ acentric factor

Subscripts
$\mathrm{C} \quad$ critical
$1 \quad \mathrm{CO}_{2}$
2 1-phenylethanol or 2-octanol

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